

## **Cambridge International Examinations**

Cambridge International General Certificate of Secondary Education

CANDIDATE NAME			
CENTRE NUMBER		CANDIDATE NUMBER	
MATHEMATICS			0580/42
Paper 4 (Extended)		Oct	tober/November 2015
			2 hours 30 minutes
Candidates answer or	n the Question Paper.		
Additional Materials:	Electronic calculator Tracing paper (optional)	Geometrical instrumer	nts

## **READ THESE INSTRUCTIONS FIRST**

Write your Centre number, candidate number and name on all the work you hand in.

Write in dark blue or black pen.

You may use an HB pencil for any diagrams or graphs.

Do not use staples, paper clips, glue or correction fluid.

DO NOT WRITE IN ANY BARCODES.

Answer all questions.

If working is needed for any question it must be shown below that question.

Electronic calculators should be used.

If the degree of accuracy is not specified in the question, and if the answer is not exact, give the answer to three significant figures. Give answers in degrees to one decimal place.

For  $\pi$ , use either your calculator value or 3.142.

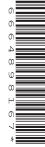
At the end of the examination, fasten all your work securely together.

The number of marks is given in brackets [ ] at the end of each question or part question.

The total of the marks for this paper is 130.

The syllabus is approved for use in England, Wales and Northern Ireland as a Cambridge International Level 1/Level 2 Certificate.





1

		rs are in the ratio men: women: children = 7:11:14.	
(a)	(i)	Show that there are 224 children in the film.	
		Answer(a)(i)	
			[2]
	(ii)	Find the number of men in the film.	
		<i>Answer(a)</i> (ii)	[1]
(b)		ry working day, each child is given \$1 to spend. h child works for 45 days.	
		culate the total amount that the film company gives the children to spend. e your answer correct to the nearest \$100.	
		Answer(b) \$	<b>[</b> 2]
(-)	TI		<u>[</u> 2]
(c)		children have lessons every day in groups of no more than 12.	
	Calo	culate the smallest possible number of groups.	
		Answer(c)	[2]
(d)	The	film costs four million and ninety three thousand dollars to make.	
	(i)	Write this number in figures.	
		<i>Answer(d)</i> (i)	[1]
	(ii)	Write your answer to part (d)(i) in standard form.	
		<i>Answer(d)</i> (ii)	[1]
(e)		VD copy of the film costs \$2.75 to make. selling price is \$8.20.	
	Calo	culate the percentage profit.	

Answer(e) ......% [3]

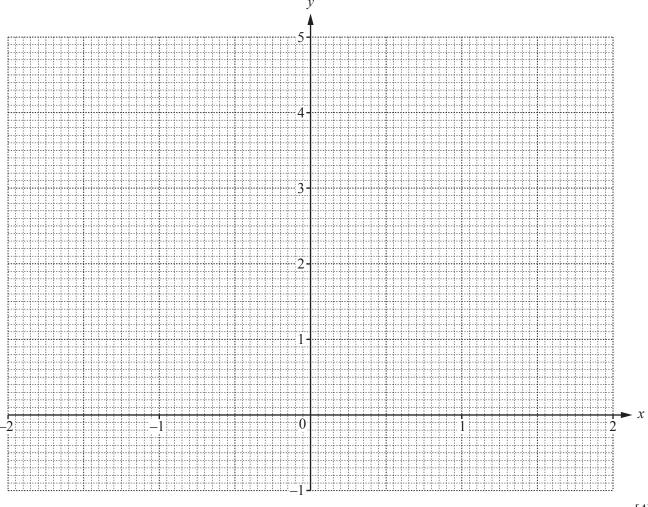
2 The table shows some values for  $y = x^3 - 3x + 2$ .

x	-2	-1.5	-1	-0.5	0	0.5	1	1.5	2
У		3.125		3.375	2		0		4

(a) Complete the table of values.

[4]

**(b)** On the grid, draw the graph of  $y = x^3 - 3x + 2$  for  $-2 \le x \le 2$ .



[4]

(c) By drawing a suitable line, solve the equation  $x^3 - 3x + 2 = x + 1$  for  $-2 \le x \le 2$ .

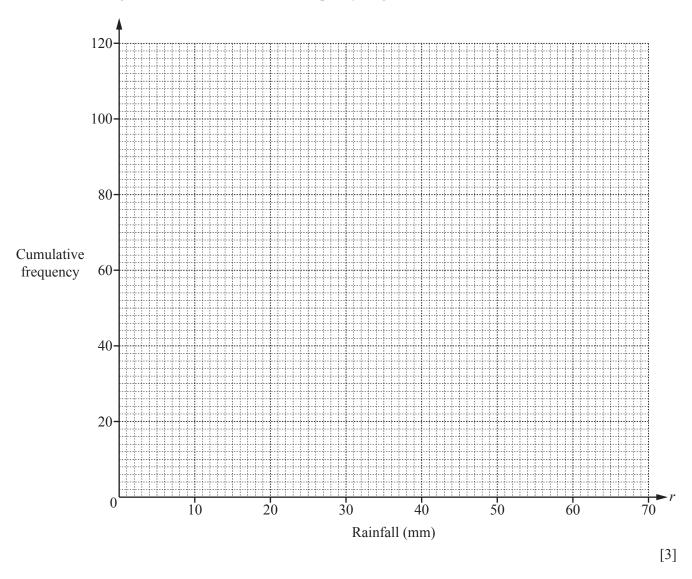
Answer(c) x = ..... or x = ..... [3]

(d) By drawing a suitable tangent, find an estimate of the gradient of the curve at the point where x = -1.5.

3 Leo measured the rainfall each day, in millimetres, for 120 days. The cumulative frequency table shows the results.

Rainfall (r mm)	r ≤ 20	r ≤ 25	<i>r</i> ≤ 35	r ≤ 40	r ≤ 60	<i>r</i> ≤ 70
Cumulative frequency	5	13	72	90	117	120

(a) On the grid below, draw a cumulative frequency diagram to show these results.



**(b) (i)** Find the median.

*Answer(b)*(i) ..... mm [1]

(ii) Use your diagram to find the number of days when the rainfall was more than 50 mm.

Answer(b)(ii) ......[2]

(c) Use the information in the cumulative frequency table to complete the frequency table below.

Rainfall (r mm)	$0 < r \le 20$	$20 < r \le 25$	$25 < r \le 35$	$35 < r \le 40$	$40 < r \le 60$	$60 < r \le 70$
Frequency	5		59			3

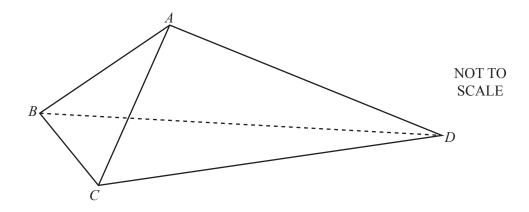
[2]

(d)	Use your frequency table to calculate an estimate of the mean
	You must show all your working.

(e) In a histogram drawn to show the information in the table in **part** (c), the frequency density for the interval  $25 < r \le 35$  is 5.9.

Calculate the frequency density for the intervals  $20 < r \le 25$ ,  $40 < r \le 60$  and  $60 < r \le 70$ .

 4



The diagram shows a tent ABCD.

The front of the tent is an isosceles triangle ABC, with AB = AC.

The sides of the tent are congruent triangles ABD and ACD.

(a) BC = 1.2 m and angle  $ABC = 68^{\circ}$ .

Find AC.

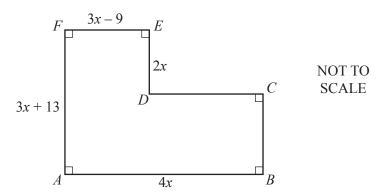
Answer(a) 
$$AC = \dots m[3]$$

**(b)**  $CD = 2.3 \,\text{m}$  and  $AD = 1.9 \,\text{m}$ .

Find angle ADC.

(c)	The floor of the tent, triangle $BCD$ , is also an isosceles triangle with $BD = CD$ .
	Calculate the area of the floor of the tent.
	$Answer(c) \qquadm^2 [4]$
(d)	When the tent is on horizontal ground, $A$ is a vertical distance 1.25 m above the ground.
	Calculate the angle between $AD$ and the ground.
	$Answer(d) \qquad [3]$

5 (a) The area of shape *ABCDEF* is 24 cm<sup>2</sup>. All lengths are in centimetres.



(i) Show that  $5x^2 + 17x - 12 = 0$ .

Answer(a)(i)

[3]

(ii) Solve, by factorising, the equation  $5x^2 + 17x - 12 = 0$ . You must show all your working.

Answer(a)(ii) 
$$x = .....$$
 or  $x = .....$  [3]

(b)	Solve the simultaneous equations.
	You must show all your working.

our working. 
$$3x - 2y = 23$$
$$-4x - y = -5$$

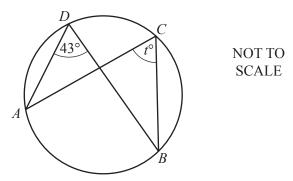
Answer(b) 
$$x = \dots$$
 [3]

(c) Solve the equation.

$$\frac{2(t+3)}{t} - \frac{t}{t+3} = 1$$

$$Answer(c) t = \dots [5]$$

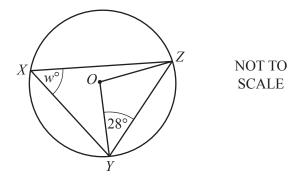
6 (a) (i) A, B, C and D lie on the circumference of the circle.



Find the value of *t*.

Answer(a)(i) t =	:	Γ	1	
11.00,000,000,000,000,000			-	

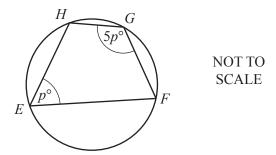
(ii) X, Y and Z lie on the circumference of the circle, centre O.



Find the value of w, giving reasons for your answer.

<i>Answer(a)</i> (11)	$w = \dots$	because	
• • • • • • • • • • • • • • • • • • • •			
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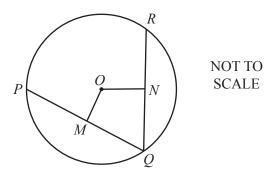
(iii) E, F, G and H lie on the circumference of the circle.



Find the value of *p*, giving a reason for your answer.

Answer(a)(iii) p =	=	because	
		[3	3]

**(b)** 



The diagram shows a circle, centre *O*. *PQ* and *QR* are chords.

*OM* is the perpendicular from *O* to *PQ*.

(i) Complete the statement.

$$PM: PQ = \dots$$
 [1]

[4]

(ii) ON is the perpendicular from O to QR and PQ = QR.

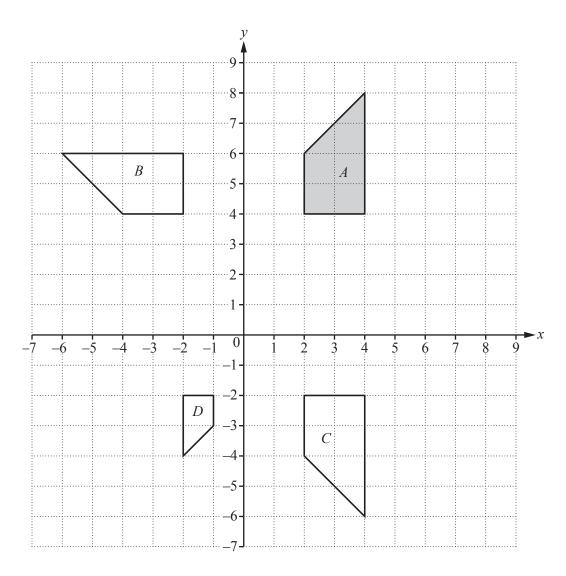
Complete the statements to show that triangle *OMQ* is congruent to triangle *ONQ*.

..... is a common side.

..... because M is the midpoint of PQ and N is the midpoint of RQ.

..... because equal chords are equidistant from ......

7



- (a) Describe fully the **single** transformation that maps
  - (i) shape A onto shape B,

Answer(a)(1)	
	Г3

(ii) shape A onto shape C,

Answer(a)(11)	 	 	 	
				-12

(iii) shape A onto shape D.



1	h)	Find the $2 \times$	2 matrix	that ren	recents th	e transform	ation in	nart (	(a)(iii	١
I	U.	rina me 2 ×	2 IIIau IX	mai rep	nesents th	e nansionii	auon m	part (	a)(III	J.

Answer(b)	[2]

- (c) On the grid, draw the image of shape A after a translation by the vector  $\begin{pmatrix} 2 \\ -3 \end{pmatrix}$ . [2]
- (d) Describe fully the **single** transformation represented by the matrix  $\begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$ .

  Answer(d)

	A lir	ne $AB$ joins the points $A$ (3, 4) and $B$ (5, 8).	
(	(a)	Write down the co-ordinates of the midpoint of the line <i>AB</i> .	
(	(b)	Answer(a) ( ) [	2
	(c)	$Answer(b) \ AB = \dots$ Find the equation of the line $AB$ .	3]
		Answer(c)	3]
	(d)	A line perpendicular to $AB$ passes through the origin and through the point $(6, r)$ . Find the value of $r$ .	
			3]

				15			
9		f(x) =	2x + 5	$g(x) = 2^x$	h(x) = 7 - 3x		
	(a)	Find					
		(i) f(3),					
					Answer(a)(i)	[1	]
		(ii) gg(3).					
					Answer(a)(ii)	ſſ	7
	(b)	Find $f^{-1}(x)$ .			Answer (u)(11)	[2	ر،
	(-)	- (-)-					
				Ang	$ver(b) f^{-1}(x) = \dots$	17	7
	(c)	Find $fh(x)$ , giving	your answer in its si		ver(0) 1 (x) –	[2	۱,
	(0)	1 ma 1 m(w), giving	your unswer in its si	imprest form.			

*Answer(c)* ..... [2]

(d) Find the integer values of x which satisfy this inequality.

$$1 < f(x) \le 9$$

10 The table shows the first five terms of sequences A, B and C.

Sequence	1st term	2nd term	3rd term	4th term	5th term	6th term
A	3	4	5	6	7	
В	0	1	4	9	16	
С	-3	-3	-1	3	9	

(a)	Complete the table for the 6th term of each sequence.	
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[2]

**(b)** Write down the *n*th term of sequence A.

Answer(b)	)	[1]	l
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(c) (i) Find the *n*th term of sequence B.

(ii) Find the value of n when the nth term of sequence B is 8281.

$$Answer(c)(ii) \quad n = \dots$$
 [2]

(d) (i) Find the *n*th term of sequence C in its simplest form.

(ii) Find the 8th term of sequence C.

(e) The *n*th term of another sequence D is  $\left(-\frac{1}{2}\right)^{n-1}$ .

Complete the table for the first four terms of sequence D.

Sequence	1st term	2nd term	3rd term	4th term
D				

[3]

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