UNIVERSITY OF CAMBRIDGE INTERNATIONAL EXAMINATIONS

GCE Advanced Subsidiary Level and GCE Advanced Level

MARK SCHEME for the October/November 2007 question paper

9709 MATHEMATICS

9709/03

Paper 3, maximum raw mark 75

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began.

All Examiners are instructed that alternative correct answers and unexpected approaches in candidates' scripts must be given marks that fairly reflect the relevant knowledge and skills demonstrated.

Mark schemes must be read in conjunction with the question papers and the report on the examination.

• CIE will not enter into discussions or correspondence in connection with these mark schemes.

CIE is publishing the mark schemes for the October/November 2007 question papers for most IGCSE, GCE Advanced Level and Advanced Subsidiary Level syllabuses and some Ordinary Level syllabuses.



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Mark Scheme Notes

Marks are of the following three types:

- M Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.
- A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).
- B Mark for a correct result or statement independent of method marks.
- When a part of a question has two or more "method" steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly when there are several B marks allocated. The notation DM or DB (or dep*) is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.
- The symbol √ implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only. A and B marks are not given for fortuitously "correct" answers or results obtained from incorrect working.
- Note: B2 or A2 means that the candidate can earn 2 or 0.
 B2/1/0 means that the candidate can earn anything from 0 to 2.

The marks indicated in the scheme may not be subdivided. If there is genuine doubt whether a candidate has earned a mark, allow the candidate the benefit of the doubt. Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored.

- Wrong or missing units in an answer should not lead to the loss of a mark unless the scheme specifically indicates otherwise.
- For a numerical answer, allow the A or B mark if a value is obtained which is correct to 3 s.f., or which would be correct to 3 s.f. if rounded (1 d.p. in the case of an angle). As stated above, an A or B mark is not given if a correct numerical answer arises fortuitously from incorrect working. For Mechanics questions, allow A or B marks for correct answers which arise from taking *g* equal to 9.8 or 9.81 instead of 10.

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The following abbreviations may be used in a mark scheme or used on the scripts:

AEF	Any Equivalent Form (of answer is equally acceptable)
AG	Answer Given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid)
BOD	Benefit of Doubt (allowed when the validity of a solution may not be absolutely clear)
CAO	Correct Answer Only (emphasising that no "follow through" from a previous error is allowed)
CWO	Correct Working Only - often written by a 'fortuitous' answer
ISW	Ignore Subsequent Working
MR	Misread
PA	Premature Approximation (resulting in basically correct work that is insufficiently accurate)
sos	See Other Solution (the candidate makes a better attempt at the same question)
SR	Special Ruling (detailing the mark to be given for a specific wrong solution, or a case where some standard marking practice is to be varied in the light of a particular circumstance)

Penalties

- MR -1 A penalty of MR -1 is deducted from A or B marks when the data of a question or part question are genuinely misread and the object and difficulty of the question remain unaltered. In this case all A and B marks then become "follow through $\sqrt{}$ " marks. MR is not applied when the candidate misreads his own figures this is regarded as an error in accuracy. An MR-2 penalty may be applied in particular cases if agreed at the coordination meeting.
- PA -1 This is deducted from A or B marks in the case of premature approximation. The PA -1 penalty is usually discussed at the meeting.

		·	
1	Obtain indefinite integral of the form $a\ln(2x-1)$, where $a=\frac{1}{2}$, 1, or 2	M1	
	Use limits and obtain equation $\frac{1}{2}\ln(2k-1) = 1$	A1	
	Use correct method for solving an equation of the form $a\ln(2k-1) = 1$, where $a = \frac{1}{2}$, 1	, or 2, for k M1	
	Obtain answer $k = \frac{1}{2}(e^2 + 1)$, or exact equivalent	A1	[4]
2	EITHER: Attempt division by $x^2 + x + 2$ reaching a partial quotient of $x^2 + kx$	M1	
	Complete the division and obtain quotient $x^2 - x + 2$	A1	
	Equate constant remainder to zero and solve for a	M1	
	Obtain answer $a = 4$ OR: Calling the unknown factor $x^2 + bx + c$, obtain an equation in b and/or c , or s	A1	
	OR: Calling the unknown factor $x^2 + bx + c$, obtain an equation in b and/or c, or s working two coefficients with the correct moduli	M1	
	Obtain factor $x^2 - x + 2$	A1	
	Use $a = 2c$ to find a	M1	
	Obtain answer $a = 4$	A1	[4]
3	Using 1 and $\ln x$ as parts reach $x \ln x \pm \int x \cdot \frac{1}{x} dx$	M1*	
	Obtain indefinite integral $x \ln x - x$	A1	
	Substitute correct limits correctly	M1(dep*)	
	Obtain given answer	A1	[4]
4	(i) Use correct product or quotient rule	M1	
	Obtain derivative in any correct form Equate derivative to zero and solve for <i>x</i>	A1 M1	
	Obtain answer $x = \frac{1}{4}\pi$ or 0.785 with no errors seen	A1	[4]
	(ii) Use an appropriate method for determining the nature of a stationary point	M1	
	Show the point is a maximum point with no errors seen [SR: for the answer 45° deduct final A1 in part (i), and deduct A1 in part (ii) if this used in the exponential.]	A1 value in degrees is	[2]
5	(i) Use correct $tan(A + B)$ formula to obtain an equation in $tan x$	M1*	
	Use tan 45° = 1 Obtain the given answer	M1(dep*)	[3]
	(ii) Make reasonable attempt to solve the given quadratic for one value of $\tan x$	M1	
	Obtain $\tan x = -1 \pm \sqrt{2}$, or equivalent in the form $(a \pm \sqrt{b})/c$ (accept 0.4, -2.4)	A1	
	Obtain answer $x = 22.5^{\circ}$	A1	
	Obtain second answer $x = 112.5$ and no others in the range [Ignore answers outside the range.] [Treat answers in radians as a MR and deduct one mark from the marks for the angular contents of the range.]	A1	[4]

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Paper 03

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· (*)				
6 (i)		ecognisable sketch of an appropriate graph, e.g. $y = \ln x$ appropriate second graph, e.g. $y = 2 - x$, correctly and justify the given statement	B1 B1	[2
(ii`) Consider	sign of $2-x-\ln x$ when $x=1.4$ and $x=1.7$, or equivalent	M1	
()		e the argument with correct calculations	A1	[2
(iii)) Rearrang	e the equation $x = \frac{1}{3}(4 + x - 2\ln x)$ as $2 - x = \ln x$, or vice versa	B1	[1
(:)) Haa tha it	counting formanile compatity at least ones	M1	
(IV)		rerative formula correctly at least once nal answer 1.56	A1	
	Show suf	ficient iterations to 4 d.p. to justify its accuracy to 2 d.p., or show there is a sign change in ral (1.555, 1.565)	A1	[3
7 (i)		variables correctly and attempt integration of both sides $m \ln N$, or equivalent	M1* A1	
	Obtain ter	rm $\frac{k}{0.02}\sin(0.02t)$, or equivalent	A1	
		$N = 125$ to evaluate a constant, or as limits, in a solution containing terms of the form $a \ln a$		
		0.02t), or equivalent	M1	r #=
	Obtain an	y correct form of solution, e.g. $\ln N = 50k\sin(0.02t) + \ln 125$	A1	[5
(ii)			1(dep*)	
	Obtain <i>k</i> =	= 0.0100479(accept $k = 0.01$)	A1	[2
		1.1. 1. 1. 1.05 (0.500 1.00.00)	D.1	
(iii) Rearrange	e and obtain $N = 125 \exp(0.502 \sin(0.02t))$, or equivalent	B1	
(iii	Set sin(0.0	O(2t) = -1 in the expression for N, or equivalent	M1	
(iii	Set sin(0.0 Obtain lea	O(2t) = -1 in the expression for N, or equivalent ast value 75.6 (accept answers in the interval [75, 76])		[3
(iii	Set sin(0.0 Obtain lea	O(2t) = -1 in the expression for N, or equivalent	M1	[3
	Set sin(0.0 Obtain lea [For the B	(02t) = -1 in the expression for N , or equivalent ast value 75.6 (accept answers in the interval [75, 76]) 81, accept 0.5 following $k = 0.01$, and allow 4.8 or better for ln 125.] ER: Carry out multiplication of numerator and denominator by $1 + 2i$, or equivalent	M1 A1	[3
	Set sin(0.0 Obtain lea [For the B	(02t) = -1 in the expression for N , or equivalent ast value 75.6 (accept answers in the interval [75, 76]) 81, accept 0.5 following $k = 0.01$, and allow 4.8 or better for ln 125.] ER: Carry out multiplication of numerator and denominator by $1 + 2i$, or equivalent Obtain answer $2 + i$, or any equivalent of the form $(a + ib)/c$	M1 A1 M1 A1	[3
	Set sin(0.0 Obtain lea [For the B	 (22t) = -1 in the expression for N, or equivalent ast value 75.6 (accept answers in the interval [75, 76]) (31) accept 0.5 following k = 0.01, and allow 4.8 or better for ln 125.] (32) ER: Carry out multiplication of numerator and denominator by 1 + 2i, or equivalent Obtain answer 2 + i, or any equivalent of the form (a + ib)/c Obtain two equations in x and y, and solve for x or for y 	M1 A1 M1 A1 M1	[3
	Set sin(0.0 Obtain lear [For the Base] (i) (i) EITHA	 (22t) = -1 in the expression for N, or equivalent ast value 75.6 (accept answers in the interval [75, 76]) (31) accept 0.5 following k = 0.01, and allow 4.8 or better for ln 125.] (32) ER: Carry out multiplication of numerator and denominator by 1 + 2i, or equivalent Obtain answer 2 + i, or any equivalent of the form (a + ib)/c Obtain two equations in x and y, and solve for x or for y Obtain answer 2 + i, or equivalent 	M1 A1 M1 A1 M1	[3
	Set sin(0.0 Obtain lea [For the B	 (22t) = -1 in the expression for N, or equivalent ast value 75.6 (accept answers in the interval [75, 76]) (31) accept 0.5 following k = 0.01, and allow 4.8 or better for ln 125.] (32) ER: Carry out multiplication of numerator and denominator by 1 + 2i, or equivalent Obtain answer 2 + i, or any equivalent of the form (a + ib)/c Obtain two equations in x and y, and solve for x or for y 	M1 A1 M1 A1 M1	[3
	Set sin(0.0 Obtain lear [For the Bank) (i) EITHAN OR1:	 (02t) = -1 in the expression for N, or equivalent ast value 75.6 (accept answers in the interval [75, 76]) (31, accept 0.5 following k = 0.01, and allow 4.8 or better for ln 125.] (21) ER: Carry out multiplication of numerator and denominator by 1 + 2i, or equivalent Obtain answer 2 + i, or any equivalent of the form (a + ib)/c Obtain two equations in x and y, and solve for x or for y Obtain answer 2 + i, or equivalent Using the correct processes express z in polar form 	M1 A1 M1 A1 M1 A1	
	Set sin(0.0 Obtain lease [For the Base] (i) (i) EITHA OR1: OR2:	 (02t) = -1 in the expression for N, or equivalent ast value 75.6 (accept answers in the interval [75, 76]) (31, accept 0.5 following k = 0.01, and allow 4.8 or better for ln 125.] (31) ER: Carry out multiplication of numerator and denominator by 1 + 2i, or equivalent Obtain answer 2 + i, or any equivalent of the form (a + ib)/c Obtain two equations in x and y, and solve for x or for y Obtain answer 2 + i, or equivalent Using the correct processes express z in polar form Obtain answer 2 + i, or equivalent 	M1 A1 M1 A1 M1 A1	
3 (a	Set sin(0.0 Obtain lea [For the Band (i) EITHA OR1: OR2: (ii) State State	(02t) = -1 in the expression for N , or equivalent ast value 75.6 (accept answers in the interval [75, 76]) (01) = -1 in the expression for N , or equivalent [75, 76]) (01) = -1 in the expression for N , or equivalent [75, 76]) (01) = -1 in the expression for N , or equivalent [75, 76]) (01) = -1 in the expression for N , or equivalent as $(0.5) = -1$ in the interval [75, 76]) (0.5) = -1 in the expression for N , or equivalent as $(0.5) = -1$ in the interval [75, 76]) (0.5) = -1 in the expression for N , or equivalent as $(0.5) = -1$ in the interval [75, 76]) (0.5) = -1 in the expression for N , or equivalent as $(0.5) = -1$ in the interval [75, 76]) (0.5) = -1 in the expression for N , or equivalent as $(0.5) = -1$ in the expression for $(0.5) = -1$ in the interval [75, 76]) (0.5) = -1 in the expression for $(0.5) = -1$ in the interval [75, 76]) (0.5) = -1 in the expression for $(0.5) = -1$ in the interval [75, 76]) (0.5) = -1 in the expression for $(0.5) = -1$ in the interval [75, 76]) (0.5) = -1 in the expression for $(0.5) = -1$ in the interval [75, 76]) (0.5) = -1 in the interval [75, 76]	M1 A1 M1 A1 M1 A1 M1 A1	[2
3 (a	Set sin(0.0 Obtain lea [For the Band (i) EITHA OR1: OR2: (ii) State State	(02t) = -1 in the expression for N , or equivalent ast value 75.6 (accept answers in the interval [75, 76]) (1) , accept 0.5 following $k = 0.01$, and allow 4.8 or better for ln 125.] ER: Carry out multiplication of numerator and denominator by $1 + 2i$, or equivalent Obtain answer $2 + i$, or any equivalent of the form $(a + ib)/c$ Obtain two equations in x and y , and solve for x or for y Obtain answer $2 + i$, or equivalent Using the correct processes express z in polar form Obtain answer $2 + i$, or equivalent that the modulus of z is $\sqrt{5}$ or 2.24	M1 A1 M1 A1 M1 A1 B1 B1	[2
3 (a	Set sin(0.0 Obtain lea [For the Band (i) EITHA OR1: OR2: (ii) State State	 D2t) = -1 in the expression for N, or equivalent ast value 75.6 (accept answers in the interval [75, 76]) B1, accept 0.5 following k = 0.01, and allow 4.8 or better for ln 125.] ER: Carry out multiplication of numerator and denominator by 1 + 2i, or equivalent Obtain answer 2 + i, or any equivalent of the form (a + ib)/c Obtain two equations in x and y, and solve for x or for y Obtain answer 2 + i, or equivalent Using the correct processes express z in polar form Obtain answer 2 + i, or equivalent that the modulus of z is √5 or 2.24 that the argument of z is 0.464 or 26.6° Square x + iy and equate real and imaginary parts to 5 and -12 respectively 	M1 A1 M1 A1 M1 A1 B1 B1	[2
3 (a	Set sin(0.0 Obtain lea [For the Band (i) EITHA OR1: OR2: (ii) State State	(02t) = -1 in the expression for N , or equivalent ast value 75.6 (accept answers in the interval [75, 76]) (0.51) = -1 in the expression for N , or equivalent ast value 75.6 (accept answers in the interval [75, 76]) (0.51) = -1 in the expression for N , or equivalent [75, 76]) (0.51) = -1 in the expression for N , or equivalent $(0.51) = -1$ in the interval [75, 76]) (0.51) = -1 in the expression for N , or equivalent $(0.51) = -1$ in the interval [75, 76]) (0.51) = -1 in the expression for N , or equivalent $(0.51) = -1$ in the interval [75, 76]) (0.51) = -1 in the expression for N , or equivalent $(0.51) = -1$ in the interval [75, 76]) (0.51) = -1 in the expression for N , or equivalent $(0.51) = -1$ in the interval [75, 76]) (0.51) = -1 in the expression for N , or equivalent $(0.51) = -1$ in the expression for $(0.51) = -1$ in the expressio	M1 A1 M1 A1 M1 A1 B1 B1	[2
3 (a	Set sin(0.0 Obtain lea [For the Band (i) EITHA OR1: OR2: (ii) State State	$(02t) = -1$ in the expression for N , or equivalent ast value 75.6 (accept answers in the interval [75, 76]) at accept 0.5 following $k = 0.01$, and allow 4.8 or better for ln 125.] ER: Carry out multiplication of numerator and denominator by $1 + 2i$, or equivalent Obtain answer $2 + i$, or any equivalent of the form $(a + ib)/c$ Obtain two equations in x and y , and solve for x or for y Obtain answer $2 + i$, or equivalent Using the correct processes express z in polar form Obtain answer $2 + i$, or equivalent that the modulus of z is $\sqrt{5}$ or 2.24 that the argument of z is 0.464 or 26.6° ∴ Square $x + iy$ and equate real and imaginary parts to 5 and −12 respectively Obtain $x^2 - y^2 = 5$ and $2xy = -12$ Eliminate one variable and obtain an equation in the other	M1 A1 M1 A1 M1 A1 M1 A1 M1 A1 M1 A1	[2
3 (a	Set sin(0.0 Obtain lea [For the Band (i) EITHA OR1: OR2: (ii) State State	(2z) = -1 in the expression for N , or equivalent ast value 75.6 (accept answers in the interval [75, 76]) $(31) = -1$, accept 0.5 following $k = 0.01$, and allow 4.8 or better for ln 125.] ER: Carry out multiplication of numerator and denominator by 1 + 2i, or equivalent Obtain answer 2 + i, or any equivalent of the form $(a + ib)/c$ Obtain two equations in x and y , and solve for x or for y Obtain answer 2 + i, or equivalent Using the correct processes express z in polar form Obtain answer 2 + i, or equivalent that the modulus of z is $\sqrt{5}$ or 2.24 that the argument of z is 0.464 or 26.6° E Square $x + iy$ and equate real and imaginary parts to 5 and −12 respectively Obtain $x^2 - y^2 = 5$ and $2xy = -12$ Eliminate one variable and obtain an equation in the other Obtain $x^4 - 5x^2 - 36 = 0$ or $y^4 + 5y^2 - 36 = 0$, or 3-term equivalent Obtain answer 3 −2i Obtain second answer −3 + 2i and no others	M1 A1 M1 A1 M1 A1 B1 B1 M1 A1 M1 A1	[2
3 (a	Set sin(0.0 Obtain lea [For the Base] (i) (i) EITHE OR1: OR2: (ii) State State (b) EITHER	ast value 75.6 (accept answers in the interval [75, 76]) ER: Carry out multiplication of numerator and denominator by $1 + 2i$, or equivalent Obtain answer $2 + i$, or any equivalent of the form $(a + ib)/c$ Obtain two equations in x and y , and solve for x or for y Obtain answer $2 + i$, or equivalent Using the correct processes express z in polar form Obtain answer $2 + i$, or equivalent that the modulus of z is $\sqrt{5}$ or 2.24 that the argument of z is 0.464 or 26.6° Square $x + iy$ and equate real and imaginary parts to z and z respectively Obtain $z^2 - z^2 = z$ and $z^2 - z^2 = z$ and $z^2 - z^2 = z$ Eliminate one variable and obtain an equation in the other Obtain $z^2 - z^2 = z$ Obtain answer $z^2 - $	M1 A1 M1 A1 M1 A1 B1 B1 M1 A1 A1 A1 A1	[2
B (a	Set sin(0.0 Obtain lea [For the Base] (i) (i) EITHE OR1: OR2: (ii) State State (b) EITHER	(22) = −1 in the expression for N , or equivalent ast value 75.6 (accept answers in the interval [75, 76]) (31) accept 0.5 following $k = 0.01$, and allow 4.8 or better for $\ln 125$.] (31) accept 0.5 following $k = 0.01$, and allow 4.8 or better for $\ln 125$.] (32) ER : Carry out multiplication of numerator and denominator by $1 + 2i$, or equivalent Obtain answer $2 + i$, or any equivalent of the form $(a + ib)/c$ Obtain two equations in x and y , and solve for x or for y Obtain answer $2 + i$, or equivalent Using the correct processes express z in polar form Obtain answer $z + i$, or equivalent that the modulus of z is $\sqrt{5}$ or 2.24 that the argument of z is 0.464 or 26.6° (2) Square $z + iy$ and equate real and imaginary parts to 5 and $z - 12$ respectively Obtain $z - 12$ = 5 and 2 $z - 12$ = 12 Eliminate one variable and obtain an equation in the other Obtain $z - 12$ = 12 in and no others [SR: Allow a solution with $z - 12$ in others [SR: Allow a solution with $z - 12$ in others [SR: Allow a solution with $z - 12$ in others [SR: Allow a solution with $z - 12$ in other form $z - 12$ in operation of $z - 12$ in the second A1 and thus a maximum of 3/6.] Convert 5 – 12 it opolar form $z - 12$ in one of the second A1 and thus a maximum of 3/6.]	M1 A1 M1 A1 M1 A1 B1 B1 M1 A1 M1 A1 M1 A1 M1 A1	[2
B (a	Set sin(0.0 Obtain lea [For the Base] (i) (i) EITHE OR1: OR2: (ii) State State (b) EITHER	$(2z) = -1$ in the expression for N , or equivalent ast value 75.6 (accept answers in the interval [75, 76]) (a., accept 0.5 following $k = 0.01$, and allow 4.8 or better for $\ln 125$.] ER: Carry out multiplication of numerator and denominator by $1 + 2i$, or equivalent Obtain answer $2 + i$, or any equivalent of the form $(a + ib)/c$ Obtain two equations in x and y , and solve for x or for y Obtain answer $2 + i$, or equivalent Using the correct processes express z in polar form Obtain answer $2 + i$, or equivalent that the modulus of z is $\sqrt{5}$ or 2.24 that the argument of z is 0.464 or 26.6° Square $x + iy$ and equate real and imaginary parts to z and z respectively Obtain $z^2 - y^2 = z$ and $z^2 - z^2 = z$ or $z^2 - z^2 = z$ and $z^2 - z^2 = z$ or $z^2 - z^2 = z$ and $z^2 - z^2 = z$ or $z^2 - z^2 = z$ and $z^2 - z^2 = z$	M1 A1 M1 A1 M1 A1 B1 B1 M1 A1 M1 A1 M1 A1 M1 A1 M1 A1	[2
3 (a	Set sin(0.0 Obtain lea [For the Base] (i) (i) EITHE OR1: OR2: (ii) State State (b) EITHER	$(2z) = -1$ in the expression for N , or equivalent ast value 75.6 (accept answers in the interval [75, 76]) (a., accept 0.5 following $k = 0.01$, and allow 4.8 or better for $\ln 125$.] ER: Carry out multiplication of numerator and denominator by $1 + 2i$, or equivalent Obtain answer $2 + i$, or any equivalent of the form $(a + ib)/c$ Obtain two equations in x and y , and solve for x or for y Obtain answer $2 + i$, or equivalent Using the correct processes express z in polar form Obtain answer $2 + i$, or equivalent that the modulus of z is $\sqrt{5}$ or 2.24 that the argument of z is 0.464 or 26.6° Square $x + iy$ and equate real and imaginary parts to z and z respectively Obtain $z^2 - y^2 = z$ and $z^2 - z^2 = z$ and $z^2 - z^2 = z$. Eliminate one variable and obtain an equation in the other Obtain $z^4 - z^2 - z^2 = z$ or $z^4 + z^2 - z^2 = z$. Obtain answer $z^4 - z^2 = z$ and no others [SR: Allow a solution with $z^2 - z^2 = z$ and no others [SR: Allow a solution with $z^2 - z^2 = z$ and no these fact that a square root has the polar form $z^4 - z^2 = z^2 = z$.	M1 A1 M1 A1 M1 A1 B1 B1 M1 A1 M1 A1 M1 A1 M1 A1	[2

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Syllabus 9709 Paper 03

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9 (i) State or imply the form
$$\frac{A}{1-x} + \frac{B}{1+2x} + \frac{C}{2+x}$$

Use any relevant method to determine a constant

Obtain A = 1, B = 2 and C = -4

$$A1 + A1 + A1$$
 [5]

M1

(ii) Use correct method to obtain the first two terms of the expansion of $(1-x)^{-1}$, $(1+2x)^{-1}$, $(2+x)^{-1}$, or $(1+\frac{1}{2}x)^{-1}$

Obtain complete unsimplified expansions up to
$$x^2$$
 of each partial fraction

$$A1\sqrt{+}A1\sqrt{+}A1\sqrt{-}$$

Combine expansions and obtain answer $1-2x+\frac{17}{2}x^2$

[5]

[Binomial coefficients such as $\binom{-1}{2}$ are not sufficient for the M1. The f.t. is on A, B, C.]

[Apply this scheme to attempts to expand $(2-x+8x^2)(1-x)^{-1}(1+2x)^{-1}(2+x)^{-1}$, giving M1A1A1A1 for the expansions, and A1 for the final answer.]

[Allow Maclaurin, giving M1A1 $\sqrt{A1}\sqrt{for}$ f(0) = 1 and f'(0) = -2, A1 \sqrt{for} f''(0) = 17 and A1 for the final answer (f.t. is on A, B,C).]

- 10 (i) Substitute for **r** and expand the given scalar product, or correct equivalent, to obtain an equation in s

 M1

 Solve a linear equation formed from a scalar product for s

 M1
 - Obtain s = 2 and position vector $3\mathbf{i} + 2\mathbf{j} + \mathbf{k}$ for A A1 [3]
 - (ii) State or imply a normal vector of p is 2i -3j + 6k, or equivalent
 Use the correct process for evaluating a relevant scalar product, e.g. (i 2j + 2k).(2i -3j + 6k)
 Using the correct process for calculating the moduli, divide the scalar product by the product of the moduli and evaluate the inverse sine or cosine of the result
 Obtain final answer 72.2° or 1.26 radians
 A1 [4]
 - Obtain final answer 72.2° or 1.26 radians

 A1

 (iii) EITHER: Taking the direction vector of the line to be $a\mathbf{i} + b\mathbf{j} + c\mathbf{k}$, state equation 2a 3b + 6c = 0B1
 - State equation a-2b+2c=0Solve to find one ratio, e.g. a:bObtain ratio a:b:c=6:2:-1, or equivalent
 - State answer $\mathbf{r} = 3\mathbf{i} + 2\mathbf{j} + \mathbf{k} + \lambda(6\mathbf{i} + 2\mathbf{j} \mathbf{k})$, or equivalent

 OR1: Attempt to calculate the vector product of a direction vector for the line l and a normal
 - Vector of the plane p, e.g.($\mathbf{i} 2\mathbf{j} + 2\mathbf{k}$)×($2\mathbf{i} 3\mathbf{j} + 6\mathbf{k}$)

 Obtain two correct components of the product

 Obtain answer $-6\mathbf{i} 2\mathbf{j} + \mathbf{k}$, or equivalent

 A1
 - State answer $\mathbf{r} = 3\mathbf{i} + 2\mathbf{j} + \mathbf{k} + \lambda(-6\mathbf{i} 2\mathbf{j} + \mathbf{k})$, or equivalent A1 $\sqrt{OR2}$: Obtain the equation of the plane containing A and perpendicular to the line l M1
 - State answer x 2y + 2z = 1, or equivalent
 Find position vector of a second point B on the line of intersection of this plane with
 - Find position vector of a second point B on the line of intersection of this plane with the plane p, e.g. $9\mathbf{i} + 4\mathbf{j}$ M1
 - Obtain a direction vector for this line of intersection, e.g. $6\mathbf{i} + 2\mathbf{j} \mathbf{k}$ State answer $\mathbf{r} = 3\mathbf{i} + 2\mathbf{i} + \mathbf{k} + 2(6\mathbf{i} + 2\mathbf{i} \mathbf{k})$ or against the state of the sta
 - State answer $\mathbf{r} = 3\mathbf{i} + 2\mathbf{j} + \mathbf{k} + \lambda(6\mathbf{i} + 2\mathbf{j} \mathbf{k})$, or equivalent [The f.t. is on A.]

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